STUDENT VERSION
MODELING THE STEEPING OF
SOUTHERN SWEET ICED TEA

Troy Henderson

Department of Mathematics

University of Mobile

Mobile AL USA

STATEMENT

There are many preferences among Southerners regarding iced tea. Some prefer unsweetened iced tea, but most prefer sweet tea. Among those that prefer sweet tea, the preferred sweetness varies. Some like to sweeten their iced tea with artificial sweeteners. Among those that use sugar to sweeten their tea, some like lightly sweetened iced tea, others like moderately sweetened, and still others like their tea extremely sweet. That is, the preference of sugar concentration is probably the biggest difference between different sweet teas.

Another difference between iced teas is the type of tea used in brewing. There are instant teas, iced tea mixes, flavored teas, decaffeinated teas, cold brew tea bags, and classic fresh brew tea bags. Yet another preference Southerners have among their ice teas is the brand of tea. Some of the most common brands are Lipton,[®] Luzianne,[®] Red Diamond,[®] and Tetley.[®]

Figure 1. Lipton[®] Family Size Tea Bags

Figure 2. Manufacturer's brewing directions

The following directions are used by the author when brewing sweet tea. The number of tea bags used and brewing time are the primary differences between these and the manufacturer's directions.

Directions

Bring $9\frac{1}{2}$ cups of water to a boil. Pour boiling water onto $1\frac{1}{3}$ cups of granulated sugar, and stir until the sugar has dissolved. Bob two Lipton® family size tea bags (see Figures 1 and 2 for package images) in the water several (10-12) times. Let the tea steep for about an hour (or so). Remove the tea bags, and stir in 8 cups of cold water. Refrigerate for several hours (if possible) before serving.

Note: If the directions above are followed, then the total amount of water used is $17\frac{1}{2}$ cups (which is about 1.1 gallons), and thus the tea pitcher used must be able to sustain this capacity. It is also worth noting that the sugar concentration used is about 1.22 (or essentially $1\frac{1}{4}$) cups/gallon.

Question 1: *How long should the tea brew so that its concentration essentially reaches steady state?*

Question 2: *How does this steady state concentration compare to the concentration attained using twice the number of tea bags brewed for the manufacturer's suggested 3-5 minutes?*

In order to answer these questions, we must determine a way to quantify the concentration level of the tea. Since the color of the brewed tea gets darker the longer the tea brews, we assume that the tea concentration stabilizes when the *darkness* of the brewed tea stabilizes. To that end, we monitor the *darkness* of the tea by periodically taking photos of the brewing tea throughout the steeping process.

Data Collection

We begin our data collection by using a spotlight positioned on one side of the tea pitcher and a webcam on the opposite side. The Linux command `uvccapture` is used to periodically (i.e. every 5 seconds) take snapshots of the steeping tea using a Logitech HD Pro Webcam C910. Figure 3 shows the initial frame captured by the webcam, and demonstrates that the pitcher initially contains the sugar and no water.

A custom Perl script was written to processes a portion of an image and return a quadruplet of the form (R,G,B,L) representing the red/green/blue/luminance of this region. The output RGBL quadruplet is the average red/green/blue/luminance values of each pixel within the circular region of the image with provided center and radius. The relative luminance, L, is determined by the standard [1, p. 4] formula

$$L = 0.2126 \cdot R + 0.7152 \cdot G + 0.0722 \cdot B$$

where R, G, and B, are the red, green, and blue components, respectively. These collected R, G, and B values, as well as the computed L values, are illustrated in Figure 4 with colors red, green, blue, and black, respectively.
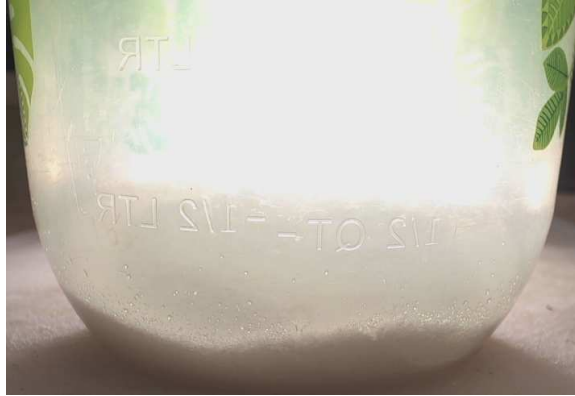
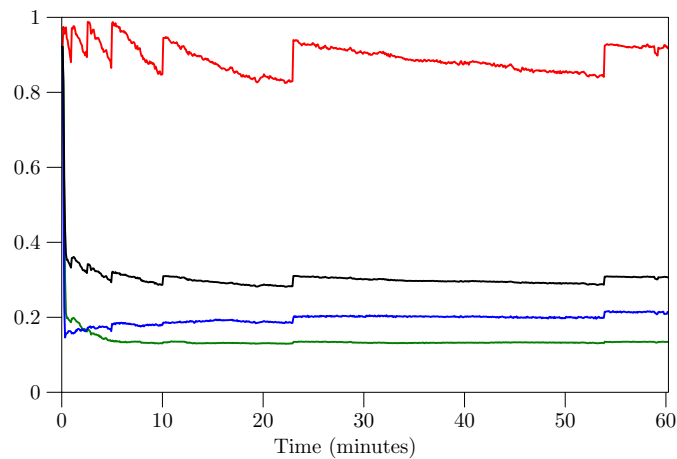**Figure 3.** Initial Frame Captured by Webcam

Figure 4. Steeping RGBL Values

Comparing the $R/G/B/L$ with the individual images captured by the webcam, it is apparent that there were several instances when the webcam automatically increased the brightness in order to provide a presumably better image. However, since these automatic adjustments are not desired for consistent data acquisition, the data was manually adjusted in order to correct this behavior. Figure 5 illustrates these corrected $R/G/B/L$ values versus time.

The initial (i.e. near $t = 0$) discontinuities for $R/G/B/L$ are due to the bobbing of the tea bags which transforms the essentially clear water (i.e. $R = G = B = L = 1$) into a darker color in a small amount of time. As the bobbing ceases, the $R/G/L$ values appear to settle into their decaying patterns, whereas the B values remain essentially constant.

The data file, file `steep.d`, is available in the Support Documents of this Modeling Scenario and contains the corrected average $R/G/B/L$ values for each time t. The data file contains 5 columns, namely (t, R, G, B, L) where each t is measured in minutes and each $R/G/B/L$ is in the interval $[0, 1]$.
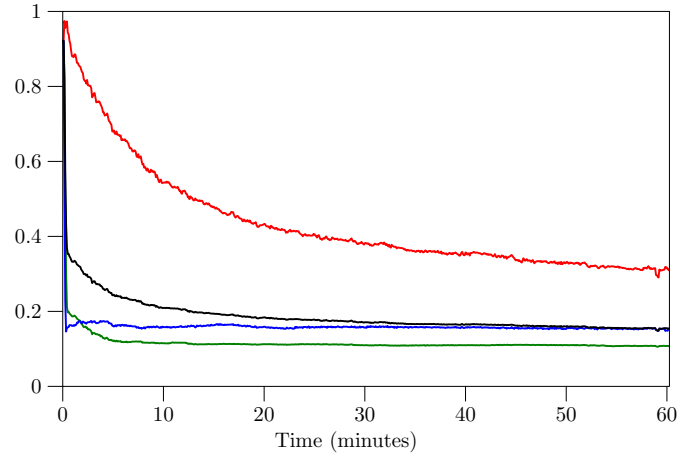
Figure 5. Repaired RGBL Values

REFERENCES

[1] Internaitonal Telecommuncation Union. 2015. Parameter values for the HDTV standards for production and international programme exchange. Recommendation ITU-R BT.709-6. `https://www.itu.int/dms_pubrec/itu-r/rec/bt/R-REC-BT.709-6-201506-I!!PDF-E.pdf`. Accessed 24 June 2016.