

Modeling Hipster Populations

PROBLEM: A

TEAM MEMBERS: JARED BEAULIEU, LYLE SMITH, JONAH TYREE

COACH: LYLE SMITH

SCHOOL: BRYAN COLLEGE

free
 $f(x)$
 inhomogeneous.

Separable: $N(y)/y = P(x)$

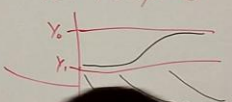
Exact: Test $\frac{\partial^2}{\partial x^2} = \frac{\partial^2}{\partial y^2}$

Bernoulli: $y' + p(x)y = y^n \quad n \neq 1$

Methods:

- Direction Fields
- Stationary Points

$() y' = M(y)$
 set $M(y) = 0$



homogeneous $y(x) = e^{\int p(x) dx} + C$

homogeneous \rightarrow find y_h
 $y = v y_h(x)$

$p(t)y = g(x)$

Modeling

- Write down everything that effects system:
- 5% Rule

$< 5\%$	$> 5\%$	} goes in model *may be pick some.
Assumption	①	
	②	
	③	
	④	
- Mathematica

The Missing Link

Problem A: Group Affinity & Fashion Sense

How do people identify with groups (hipsters specifically)?

- ▶ Model how people within groups interact and change their appearance.
- ▶ Describe how long it takes for people to change appearance.
- ▶ Analyze which parts of the model impact how subgroups change and how quickly the change occurs.

Define Hipster

- ▶ If I did, it would be too mainstream to maintain accuracy.

The Hipster

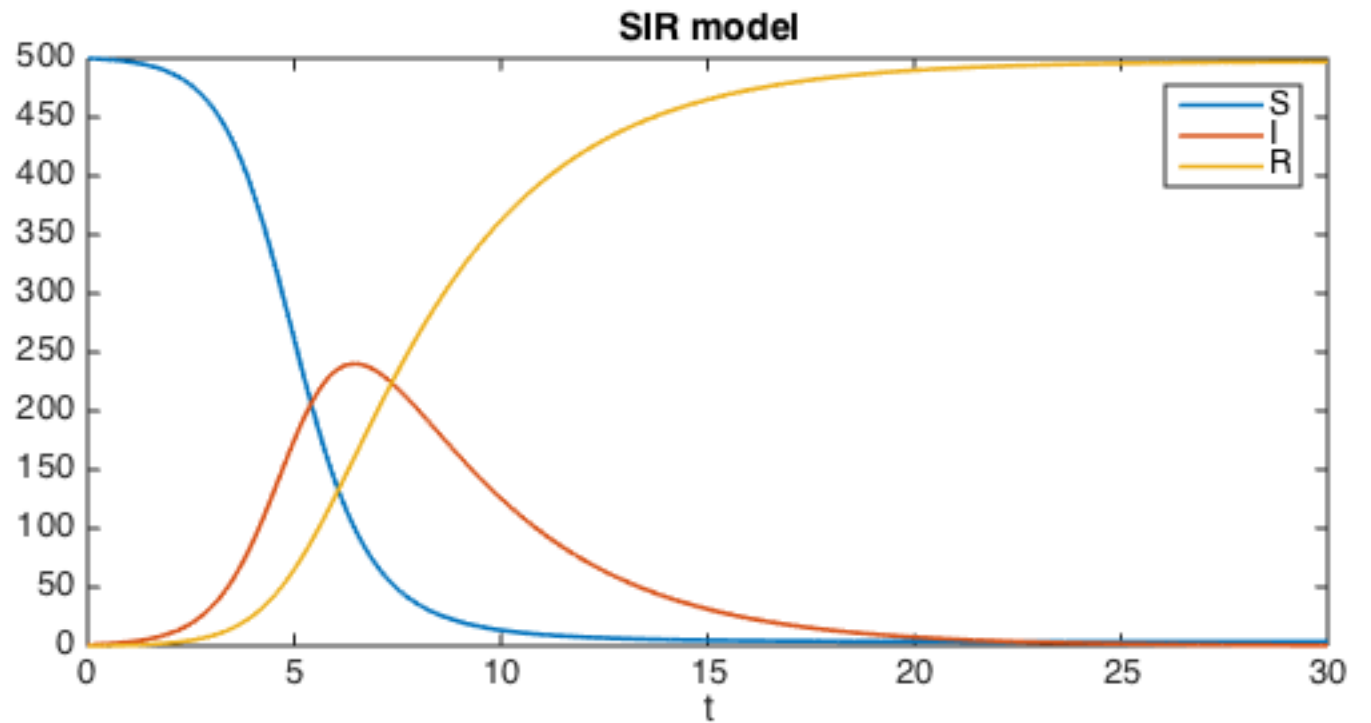


The “SIR” Model

- ▶ $S'(t) = -\mathbf{a} S(t) I(t)$
 - ▶ S: number of people susceptible to disease
- ▶ $I'(t) = \mathbf{a} S(t) I(t) - \mathbf{b} I(t)$
 - ▶ I: number of infected people
- ▶ $R'(t) = \mathbf{b} I(t)$
 - ▶ R: number of people recovered from disease

Why SIR?

- ▶ Standard epidemic model
- ▶ Models interactions between people
- ▶ Diseases analogous to social trends



Why Add to SIR?

- ▶ SIR does not account for immunity
- ▶ Why not MSIR?
 - ▶ M is temporary immunity
 - ▶ Immunity not assured until exposure
- ▶ Fixed population in SIR; does not allow for large time frames

Custom Modifications

- ▶ Add term for immunity
 - ▶ $\pm c S(t)$
 - ▶ Allow for people to move directly from S group to H group
- ▶ Changing population?
 - ▶ $+ 817.13$ to $S(t)$
 - ▶ Adds approx. 817 people every day to susceptible pool
 - ▶ Ensures model can reach beyond short-term

Our Final Equations

$$S'(t) = -a S(t) H(t) - c S(t) + 817.13$$

$$H'(t) = a S(t) H(t) - b H(t)$$

$$R'(t) = b H(t) + c S(t)$$

Assumptions

- ▶ System population: 21% of US population OR people aged 19-34
- ▶ Anyone outside age range not susceptible
- ▶ $H(0) = 25\%$ of system pop.
- ▶ $S(0) = \text{total} - H(0)$
- ▶ Higher H population means slower growth
- ▶ Hipster is binary state; either true or false
- ▶ 817 people added to $S(t)$ daily
- ▶ Hipster population follows chart of Google N-gram history of hipster
- ▶ Current day at peak; decline in future
- ▶ Hipster population never passes 50% of initial system population

Determining Constants

Recovery Constant (**b**):

- ▶ Rate at which people stop being hipsters
- ▶ Likely to leave job in approx. 2 years, 12-year period
- ▶ Likely in college 4 years, 3 of which during 19-34 age range

$$b = \frac{\left(\frac{1}{2 * 365}\right) * 12 + \left(\frac{1}{3 * 365}\right) * 3}{15 * 365} * .08$$

- ▶ Likelihood of a large-scale life change affecting hipsterism multiplied by likelihood of such an event occurring

Determining Constants

Influence Constant (**a**):

- ▶ Expected to be very small in SIR model
- ▶ Likelihood of a single interaction causing conversion to hipsterism divided by time constant of hipster transformation (1/2 year)

$$a = \frac{1}{.5 * 365} * n$$

- ▶ Solve for n ; found iteratively to be .00000000178

Determining Constants

Immunity Constant (**c**):

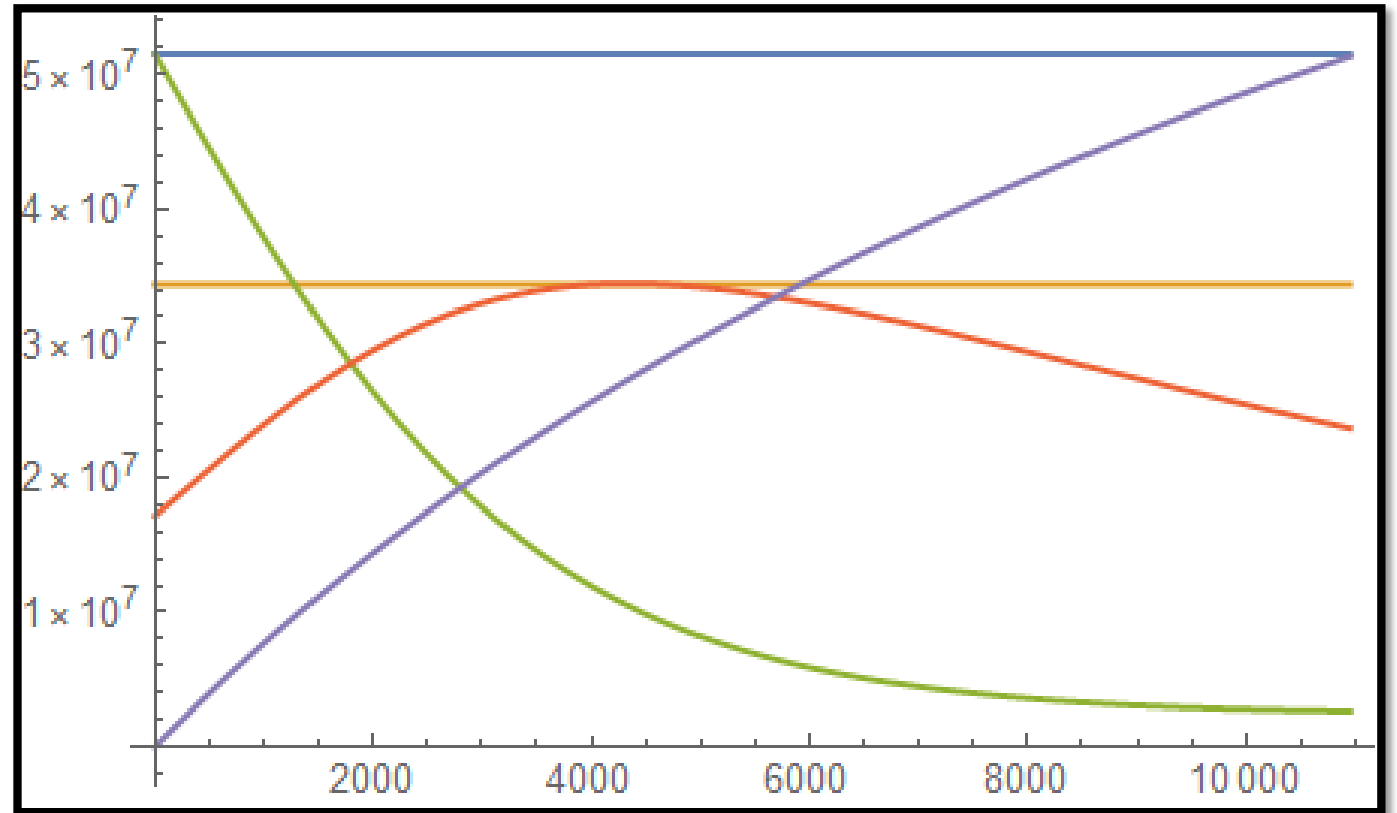
- ▶ Rate of people transferring from susceptible group straight to recovered group
- ▶ Approximately .01% of susceptible will be immune in a day

$$c = .000125$$

- ▶ Note: constants **a**, **b**, **c** designed to fit expected values for H, R

Graphing the System

- ▶ $S(t)$
- ▶ $H(t)$
- ▶ $R(t)$
- ▶ .5 Sample pop



Conclusion

- ▶ What aspect is being changed?
 - ▶ The behavior of our people groups is being changed. Specifically, their fashion sense is going from normal to hipster and (hopefully) back to normal.
- ▶ How is information exchanged between groups?
 - ▶ Everyday social interactions, social media, mass media, advertising
- ▶ Transmission rate n main goal of exercise
 - ▶ Describes rate of effectiveness per interaction in turning someone hipster, assuming hipsterization time of 1/2 year
- ▶ Values/ranges of parameters
 - ▶ What does higher **a**, **b**, **c** do?
- ▶ Backward Extrapolation
 - ▶ Very little data to find constants empirically

Additional Issue

Issue 2: The original statement asks you to model one aspect that is adopted within a group. How would your model change if you are required to model how two aspects are adopted within a group?

How would the Model Change?

- ▶ Add fourth growth constant (**d**) to system

$$S'(t) = -a S(t) H(t) - c S(t) - d S(t) H(t) + 817.13$$

$$H'(t) = a S(t) H(t) - b H(t) + d S(t) H(t)$$

$$R'(t) = b H(t) + c S(t)$$

- ▶ **a** is growth rate for first aspect (appearance); **d** is growth rate for second (lifestyle)

What do we think would happen?

- ▶ Previous constants no longer applicable; must be adjusted to conform to new expectations
- ▶ Both aspect groups combined into one “infected” group $H(t)$
 - ▶ Aspects not mutually exclusive
- ▶ $\mathbf{a} + \mathbf{d}$ should approximately equal \mathbf{a} from original model
- ▶ Gives better holistic model of hipsters; multiple aspects of hipster lifestyle, not just one
- ▶ Should fit same curves as previous model
- ▶ Values could be found through further study of hipster life

Sources Referenced

- ▶ Hipster picture: <http://www.korsgaardscommentary.com/2012/04/why-hipsters-suck.html>
- ▶ SIR picture: <https://www.chebfun.org/examples/ode-nonlin/ModellingDiseases.html>
- ▶ 21% of US from 19-34: [Kaiser Family Foundation](#)
- ▶ Google N-Gram for hipster: [Hipsters/year graph](#)